



Sheet (2) D.C. Motors

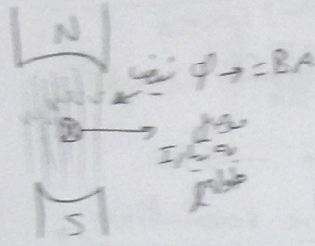
- P51 1) A 4 pole, lap wound, D.C. motor has 540 conductors. Its speed is found to be 1000 r.p.m. when it is made to run light. The flux per pole is 25 mWb. It is connected to 230 V D.C. supply. The armature resistance is 0.8Ω . Calculate:
- i) Induced e.m.f. ii) Armature current iii) Stray losses iv) Lost torque
- P62 2) A d.c. shunt motor runs at a speed of 1000 r.p.m. on no load taking a current of 6 A from the supply, when connected to 220 V d.c. supply. Its full load current is 50 A. Calculate its speed on full-load. Assume $R_a = 0.3 \Omega$ and $R_{sh} = 110 \Omega$.
- P63 3) A d.c. series motor is running with a speed of 800 r.p.m. while taking a current of 20 A from the supply. If the load is changed such that the current drawn by the motor is increased to 50 A, calculate the speed of the motor on new load. The armature and series field winding resistances are 0.2Ω and 0.3Ω respectively. Assume the flux produced is proportional to the current. Assume supply voltage as 250 V.
- P75 4) A 250 V d.c. shunt motor has a shunt field resistance of 200Ω and an armature resistance of 0.3Ω . For a given load, motor runs at 1500 r.p.m. drawing a current of 22 A from the supply. If a resistance of 150Ω is added in series with the field winding, find the new armature current and the speed. Assume load torque constant and magnetization curve to be linear.
- P80 5) A d.c. series motor runs at 500 r.p.m. on 220 V supply drawing a current of 50 A. the total resistance of the machine is 0.15Ω , calculate the value of the extra resistance to be connected in series with the motor circuit that will reduce the speed to 300 r.p.m. The load torque being half of the previous value. Assume flux proportional to the current.
- P99 6) A 500 V d.c. shunt motor runs at its normal speed of 250 r.p.m. when the armature current is 200 A. The armature resistance is 0.12Ω . Calculate the speed when a resistance is inserted in the field reducing the shunt field current to 80% of the normal value and the armature current is 100 A.

Best wishes
Course committee:
Dr. Abd Al-Wahab Hasan
Eng. Mohamed Gamal
Eng. Kotb Mohamed

①

Electrical Motor

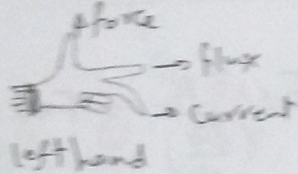
فكرة العمل: عند وضع موصل يمر به تيار كهربائي في مجال مغناطيسي فإنه هذا الموصل يتأثر بقوة تؤديه إلى تحريكه هذه القوة يعبر عنها بالقانون التالي:



$$F = B l I$$

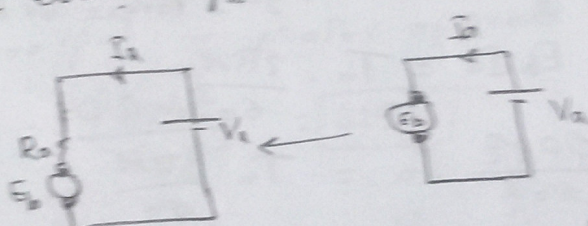
B → flux density
 l → length of conductor
 I → current passing through conductor

قيم تحديد اتجاه القوة Force بواسطة قاعدة اليد اليسرى
 أما في الرسم يتم تحديد القوة " " " " " "



مع انعكس اتجاه دوران الموتور مع عكس اتجاه المجال
 أو تغيير اتجاه التيار المار في الموصل

نتمتعش الـ back EMF من الموتور بالمعادلة الآتية $E_b = \frac{\Phi P N}{60 A}$ من الرسم ويمكن هنا back EMF أن تكونه أو تكونه من اتجاه عكس الاتجاه المسبب لتكوينها بواسطة قاعدة لينز



$$\therefore V_a = I_a R_a + E_b + V_{brush} \quad \therefore I_a = \frac{V_a - E_b}{R_a}$$

وتختلف المعادلة من ذكرين على حسب نوع الموتور

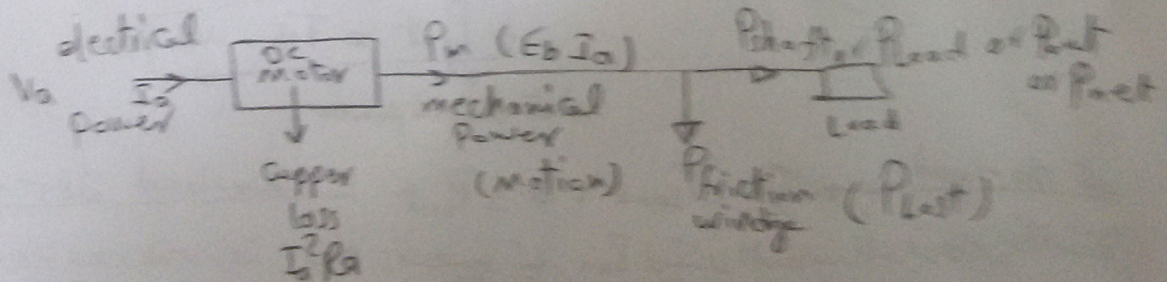
تقبل معادلة الموتور

أنواع الموتور DC

مع كتابة معادلات كل نوع لتوزيع الزخم

- Separately excited
- shunt
- series
- Compound
 - short shunt
 - long

Motor Power Equation



$$V_a = E_b + I_a R_a \times I_a \quad \therefore V_a I_a = E_b I_a + I_a^2 R_a$$

Net elec power \leftarrow $V_a I_a$ $E_b I_a$ → Gross mechanical Power (P_m) $I_a^2 R_a$ → Copper loss in Armature

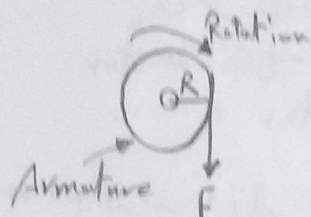
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So $P_m = \text{Power in } p\text{-Arm. Copper loss}$

← معادلة العزم في الموتور Torque Eqn.

if the motor rotate with N (rpm) speed

So angular speed $\omega = \frac{2\pi N}{60}$ rad/sec.



work done in one revolution $\rightarrow W$

$$W = F \times \text{distance in one revolution} \rightarrow 2\pi R$$

$$W = F \times 2\pi R$$

Power developed $P_d = \frac{W}{t} = \frac{F \times 2\pi R}{t} = \frac{F \times 2\pi R}{(\frac{60}{N})} = F \times R \times (\frac{2\pi N}{60})$

الطاقة الميكانيكية أو gross mech. Power

where $\omega = \frac{2\pi N}{60}$, $T = F \times R$ القوة الميكانيكية

gross mech. $\therefore P_d = T_a \cdot \omega$ gross Torque or Arm. Torque or developed Torque

$\therefore E_b I_a = T_a \cdot \frac{2\pi N}{60}$

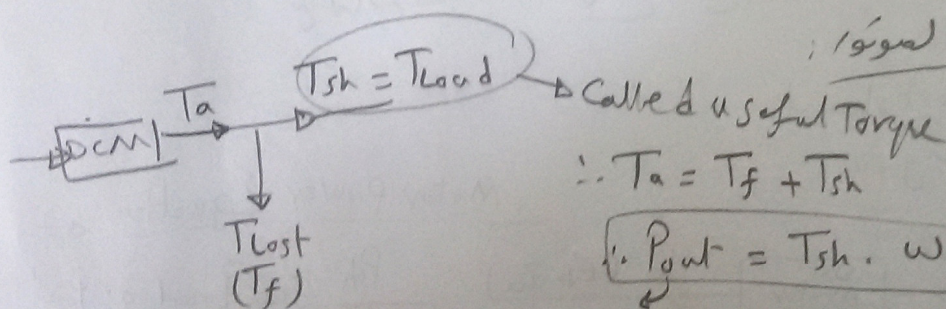
$$\frac{\phi P Z}{60 A} I_a = T_a \frac{2\pi N}{60}$$

$$\therefore T_a = \frac{1}{2\pi} \cdot I_a \cdot \phi \cdot \frac{P Z}{A}$$

Torque Equation of D.C. motor

$$\boxed{T_a = 0.159 \phi I_a \frac{P Z}{A}} \quad (\text{N.m})$$

← أنواع العزم في الموتور



$$\therefore T_a = T_f + T_{sh}$$

$$\boxed{\therefore P_{out} = T_{sh} \cdot \omega}$$

Net output power

at No-load $\rightarrow T_{sh} = T_{load} = 0 = P_{out}$ ← العزم عند no-load

لكن الموتور يدور بسرعة No ، ويجب تيار I_{a0} ليثبت المغناطيس الموجود في المجال

$$\therefore I_{a0} = \frac{V_a - E_{b0}}{R_a}$$

$I_{a0} \phi \propto T_{a0}$ التي يتسبب مع \propto

وبما أنه ϕ موجود وال I_a موجود \therefore ينتج عزم في الامل

③

$$\therefore T_{a0} \propto \phi I_{a0}$$

$$\therefore T_a = T_f + T_{Ph} \quad \therefore \boxed{T_{a0} = T_f}$$

∴ العزم الناتج عند الحمل هو العزم المفقود عند المحرك shaft

So Power developed $\boxed{E_{b0} I_{a0}}$ = friction, windage, iron losses
Called stray losses

$$\therefore T_{a0} = T_f = \frac{P_{a0}}{\omega_0} = \frac{E_{b0} I_{a0}}{\left(\frac{2\pi N_0}{60}\right)} \quad \text{N.m}$$

Problem ① $P=4, A=P=4, Z=540, N=1000 \text{ rpm}$ (when running at N_0)

$$\phi = 25 \times 10^{-3} \text{ Wb}, V_a = 230 \text{ V}, R_a = 0.8 \Omega$$

Req. $E_{b0}, I_{a0}, P_{\text{stray}}, T_f$

$N_0 \rightarrow 1000 \text{ rpm}$ ∴ Motor operate at no-load ^{المحرك}

$$\therefore E_{b0} = \frac{\phi Z N_0}{60 A} = \boxed{225 \text{ V}}$$

$$\therefore V_a = E_b + I_a R_a \rightarrow V_a = E_{b0} + I_{a0} R_a$$

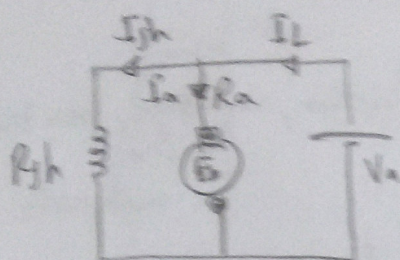
$$\therefore I_{a0} = \frac{230 - 225}{0.8} = \boxed{6.25 \text{ A}}$$

$$P_{\text{stray}} = E_{b0} I_{a0} = \boxed{1406.25 \text{ W}}$$

$$T_f = \frac{P_{\text{stray}}}{\omega_0} = \frac{P_{a0}}{\omega_0} = \frac{1406.25}{\left(\frac{2\pi \times 1000}{60}\right)} = \boxed{13.428 \text{ N.m}}$$

④
problem 2

$N_2 = 1000 \text{ rpm}$, $I_L = 6 \text{ A}$, $V_a = 220 \text{ V}$, $I_{f.L} = 50 \text{ A}$
 $N_{f.L} = ?$, $R_a = 0.3 \Omega$, $R_{sh} = 110 \Omega$



at no-load $I_{L0} = 6 \text{ A}$

$$\therefore I_{L0} = I_{a0} + I_{sh}, \quad I_{sh} = \frac{220}{110} = 2 \text{ A}$$

$$\therefore I_{a0} = 6 - 2 = 4 \text{ A}$$

$$\therefore V_a = E_{b0} + I_{a0} R_a$$

$$\therefore E_{b0} = 218.8 \text{ V}$$

at full load $I_{sh} \rightarrow \text{const.}$

$$I_{L.f.L} = 50 = I_{a.f.L} + I_{sh}$$

$$\therefore I_{a.f.L} = 50 - 2 = 48 \text{ A}$$

$$\therefore E_{b.f.L} = V_a - I_{a.f.L} R_a = 205.6 \text{ V}$$

$$\therefore E_b = \frac{\phi P N Z}{60 A} \quad \therefore N \propto \frac{E_b}{\phi} \quad \therefore N = K \frac{E_b}{\phi}$$

$$\therefore \frac{N_1}{N_2} = \frac{(E_{b1})/(\phi_1)}{(E_{b2})/(\phi_2)} \quad \text{but } \phi \text{ is const.} \rightarrow \text{shunt motor}$$

$$\therefore \frac{N_1}{N_2} = \frac{E_{b1}}{E_{b2}} \quad \therefore \frac{N_{n.L}}{N_{f.L}} = \frac{E_{b0}}{E_{b.f.L}}$$

$$\therefore N_{f.L} = \frac{E_{b.f.L}}{E_{b0}} \cdot N_{n.L}$$

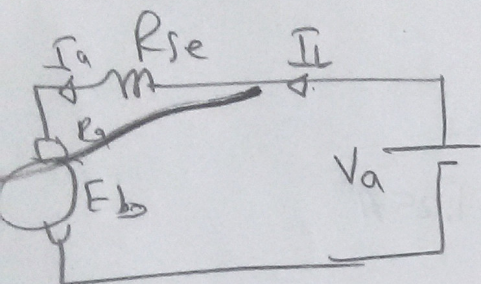
$$\therefore N_{f.L} = 939.67 \text{ rpm}$$

⑤
 Ques ③

series motor $N = 800 \text{ rpm}$, $I_L = 20 \text{ A}$

$I_{L2} = 50 \text{ A}$, $(N_2 = ?)$, $R_a = 0.2 \Omega$, $R_{se} = 0.3 \Omega$

$\phi \propto I_a, I_L$, $V_a = 250 \text{ V}$



Sol
 → For Load ① $N_1 = 800 \text{ rpm}$

$$I_{a1} = I_{L1} = 20 \text{ A}$$

$$\therefore V_a = E_b + I_a (R_a + R_{se})$$

$$\therefore E_{b1} = V_a - I_{a1} (R_a + R_{se})$$

$$\therefore E_{b1} = 240 \text{ V}$$

→ for Load ② $I_{a2} = I_{L2} = 50 \text{ A}$ $\therefore E_{b2} = V_a - I_{a2} (R_a + R_{se})$
 $\therefore N \propto \frac{E_b}{\phi}$, $\phi \propto I_a, I_L$ $E_{b2} = 225 \text{ V}$

$$\therefore \frac{N_1}{N_2} = \frac{(E_{b1} / I_{a1})}{(E_{b2} / I_{a2})} \quad \therefore \frac{N_1}{N_2} = \frac{E_{b1} \cdot I_{a2}}{E_{b2} \cdot I_{a1}}$$

$$\therefore N_2 = N_1 \cdot \frac{E_{b2} \cdot I_{a2}}{E_{b1} \cdot I_{a1}} = 800 \times \frac{225 \times 20}{240 \times 50}$$

$$\therefore N_2 = 300 \text{ rpm} \quad \#$$

problem 6

$V_a = 250V$ shunt, $R_{sh1} = 200\Omega$, $R_a = 0.3\Omega$
 $N_1 = 1500\text{rpm}$, $I_{L1} = 22A$, $R_{sh\text{new}} = 200 + 150\Omega \rightarrow I_{a\text{new}} = ?$

$N_{2\text{new}} = ?$ Assume load torque = const.

USI
 \rightarrow for the first load

$$I_{L1} = 22A = I_{a1} + I_{sh1}$$

$$I_{sh1} = \frac{V_a}{R_{sh1}} = \frac{250}{200} = 1.25A$$

$$\therefore I_{a1} = 20.75A \therefore E_{b1} = V_a - I_{a1} R_a$$

$$\therefore E_{b1} = 250 - 20.75 \times 0.3 = 243.775V$$

$$\therefore T_a = 0.159 \phi I_a \cdot \frac{PZ}{A} \therefore T_a \propto \phi I_a, \phi \propto I_{sh}$$

$$\therefore T_a \propto I_{sh} I_a \therefore \frac{T_1}{T_2} = \frac{I_{sh1} \cdot I_{a1}}{I_{sh2} \cdot I_{a2}}$$

$$\therefore \text{Said Load Torque} = \text{const} \rightarrow \therefore T_1 = T_2$$

$$\therefore I_{sh1} I_{a1} = I_{sh2} I_{a2}$$

$$I_{sh2} = \frac{V_a}{R_{sh\text{new}}} = \frac{250}{200 + 150} = 0.7142A$$

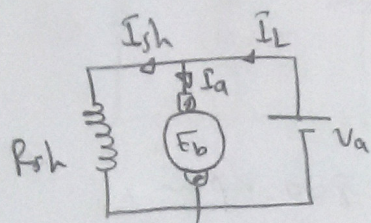
$$\therefore I_{a2} = \frac{I_{sh1} I_{a1}}{I_{sh2}} = 36.3125A$$

$$\therefore E_{b2} = V_a - I_{a2} R_a$$

$$\therefore E_{b2} = 239.1062V$$

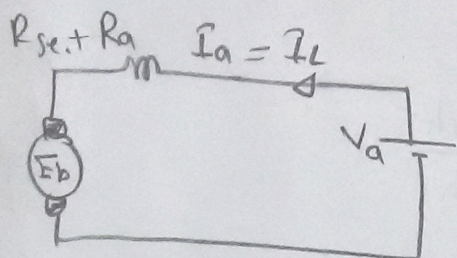
$$\therefore N \propto \frac{E_b}{\phi} \therefore \frac{N_1}{N_{2\text{new}}} = \frac{E_{b1}}{E_{b2}} \cdot \frac{I_{sh2}}{I_{sh1}}$$

$$\therefore N_{2\text{new}} = 2575.03\text{rpm} \#$$



Problem (5)

series at $N_1 = 500 \text{ rpm}$, $V_a = 220 \text{ V}$, $I_{L1} = 50 \text{ A}$
 $(R_a + R_{se}) = 0.15 \Omega$, $R_{ext.} = ? \rightarrow N_2 = 300 \text{ rpm}$
 $T_{L2} = \frac{1}{2} T_{L1}$, $\phi \propto I_a, I_L$



$$\therefore V_a = E_{b1} + I_{a1} (R_a + R_{se})$$

$$I_{a1} = I_{L1} = 50 \text{ A}$$

$$\therefore E_{b1} = 220 - 50(0.15) = \boxed{212.5 \text{ V}}$$

$$V_a = E_{b2} + I_{a2} (R_a + R_{se} + R_{ext.})$$

for computing I_{a2}

$$\therefore T \propto \phi I_a, \phi \propto I_a \therefore T \propto I_a^2$$

$$\therefore \frac{T_1}{T_2} = \frac{I_{a1}^2}{I_{a2}^2} \rightarrow \frac{T}{\frac{1}{2} T} = \frac{(50^2)}{I_{a2}^2} \therefore \boxed{I_{a2} = 35.355 \text{ A}}$$

$$\therefore \underset{220}{V_a} = E_{b2} + 35.355(0.15 + R_{ext.})$$

for computing E_{b2}

$$\therefore N \propto \frac{E_b}{\phi} \therefore \frac{N_1}{N_2} = \frac{E_{b1}}{E_{b2}} \cdot \frac{I_{a2}}{I_{a1}}$$

$$\therefore \frac{500}{300} = \frac{212.5 \times 35.355}{E_{b2} \times 50} \therefore \boxed{E_{b2} = 90.0279 \text{ V}}$$

$$\therefore 220 = 90.0279 + 35.355(0.15 + R_{ext.})$$

$$\therefore \boxed{R_{ext.} = 3.526 \Omega}$$

8) problem 6

$$V_a = 500V \text{ shunt } N_1 = 250 \text{ rpm} \rightarrow I_{a1} = 200A, R_a = 0.12\Omega$$
$$N_2 = ? \quad I_{sh2} = 80\% I_{sh1} \rightarrow I_{a2} = 100A$$

sol

$$\therefore \frac{N_1}{N_2} = \frac{E_{b1}}{E_{b2}} \cdot \left(\frac{I_{sh2}}{I_{sh1}} \right) \rightarrow \frac{0.8 I_{sh1}}{I_{sh1}}$$

$$E_{b1} = V_a - I_{a1} R_a = 500 - 200 \times 0.12 = \boxed{476V}$$

$$E_{b2} = V_a - I_{a2} R_a = 500 - 100 \times 0.12 = \boxed{488V}$$

$$\therefore \frac{250}{N_2} = \frac{476}{488} \times 0.8 \quad \therefore \boxed{N_2 = 320.378 \text{ rpm}} \#$$